



Multilateral indices and the relaunch problem

Product clustering and alternative solutions

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Relaunch problem



Relaunches

- Product replaced by (almost) identical one
- Price change often larger than quality change
- Matched-model methods miss price changes due to relaunches (if nothing is done)
- Here focus on: Geary-Khamis, TPD and GEKS-Törnqvist



Product clustering



Method

- Items combined into product clusters
- Cluster prices computed as unit values
- Unit value bias for heterogeneous items
- Crucial: Suitable cluster definition



Example: Unit value bias

| | Price (0) | Price (1) | | Quantity (0) | Quantity (1) |
|-------------------------|-----------|-----------|--|--------------|--------------|
| Product 1 | 10 | 12 |  | 100 | 300 |
| Product 2 | 18 | 20 |  | 300 | 100 |
| Unit value price | 16 | 14 |  | | |

Clustering: pros and cons

Pros

- Broad applicability
- Well established
- Easy

Cons

- Unit value bias
(heterogeneous strata)
- Analysis below cluster level
impossible (loss of details)



Imputation



Method

- Price estimated for non-sold items
- Aim: solve relaunch problem rather than to complete data -> might give interpretation problems
e.g. imputed price for a nonseasonal item
- Non-trivial choice between imputation methods
- Methods available for some indices (e.g. GEKS-Törnqvist) but less well known for others (e.g. TPD)

Relation imputation and clustering

Imputation methods exist that give the same results as product clustering

- GEKS- Törnqvist:
clustering same as imputing each price with unit value
(unobserved **and** observed prices)
- TPD and Geary-Khamis:
Same as for GEKS- Törnqvist, but also quantities need
to be imputed



Relation imputation and clustering

- Unit value bias in clustering corresponds to a rigorous imputation approach
- In paper: new imputation methods that:
 - mimic product clustering
 - less rigorous replacement of prices

If all prices are observed -> No adjustment
(contrary to clustering)

If many prices are missing -> Similar results as clustering



Product matching



Method

- Each new product matched with a disappeared product
- Replacement and replaced products should be similar
- Semi-automatic procedures proposed: text mining and manual analysis
- Automatable methods needed for transaction data
- Solution needed if number of new and disappeared products are unequal
- In paper: a simple procedure with arbitrary choices



Matching

Pros

No adjustment of prices and quantities
(contrary to clustering and imputation)

Cons

Arbitrary choices (matching procedure)

Interpretation of the matched products



Simulation



Setup

- 12 month data TV's, chocolate and potato products
- Fixed population: products that have been sold each month
- Simulated relaunches (change of product ID)
- Monte carlo simulation (100 replicates)
- Comparison:
 - no correction, clustering, imputation, matching versus 'true' index without simulated relaunches
- Criterion: median abs difference of index values



Scenario 1: random relaunches

TV's : Median distance from true index

| | GEKS-Törnqvist | Geary Khamis | TPD |
|---------------|----------------|--------------|-------------|
| No correction | 1.18 | <u>1.32</u> | <u>0.74</u> |
| Imputation | <u>0.65</u> | 4.74 | 4.83 |
| Matching | 1.38 | 1.48 | 2.33 |
| Clustering | 4.56 | 5.52 | 5.63 |

Chocolates: Median distance from true index

| | GEKS-Törnqvist | Geary Khamis | TPD |
|---------------|----------------|--------------|-------------|
| No correction | <u>0.37</u> | <u>0.16</u> | <u>0.20</u> |
| Imputation | 0.47 | 0.94 | 1.47 |
| Matching | 0.46 | 0.58 | 0.98 |
| Clustering | 0.78 | 1.07 | 1.03 |



Scenario 1: random relaunches

Potatoes: Median distance from true index

| | GEKS-Törnqvist | Geary Khamis | TPD |
|---------------|----------------|--------------|-------------|
| No correction | 1.96 | 1.40 | 1.22 |
| Imputation | 1.78 | 1.31 | 1.15 |
| Matching | <u>0.48</u> | <u>0.53</u> | <u>0.51</u> |
| Clustering | 1.27 | 1.37 | 1.37 |

- Best correction method:
 - For TV's and Chocolates: 'No correction'
 - For Potatoes: 'Matching'
- Matching always better than clustering

Scenario 2: Non-random relaunches

- Relaunches occur at one time period for randomly selected 75% of all items.
- Each relaunch goes along with a simulated, permanent price increase by 20%.



Scenario 2: Non-random relaunches

TV's: Median distance from true index

| | GEKS-Törnqvist | Geary Khamis | TPD |
|---------------|----------------|--------------|-------------|
| No correction | 11.14 | 7.39 | 10.54 |
| Imputation | <u>1.24</u> | 3.81 | 5.11 |
| Matching | 2.10 | <u>1.44</u> | <u>3.62</u> |
| Clustering | 5.63 | 6.66 | 6.70 |

Chocolates: Median distance from true index

| | GEKS-Törnqvist | Geary Khamis | TPD |
|---------------|----------------|--------------|-------------|
| No correction | 14.77 | 11.90 | 14.61 |
| Imputation | 1.83 | <u>0.34</u> | 3.04 |
| Matching | <u>0.20</u> | 4.09 | <u>0.54</u> |
| Clustering | 0.74 | 0.85 | 0.81 |



Scenario 2: Non-random relaunches

Potatoes: Median distance from true index

| | GEKS-Törnqvist | Geary Khamis | TPD |
|---------------|----------------|--------------|-------------|
| No correction | 13.33 | 10.42 | 13.40 |
| Imputation | <u>0.83</u> | 2.06 | 1.28 |
| Matching | 0.95 | 1.58 | <u>1.05</u> |
| Clustering | 1.10 | <u>1.31</u> | 1.20 |

- Correction method necessary (“no correction” gives large errors)
- Best correction method depends on data set and index method:
 - * Matching (5 cases)
 - * Imputation (3 cases)
 - * Clustering (1 case)
- Matching better than clustering for 7 out of 9 cases

Conclusion



- Correction for relaunches needed (given a price increase)
- Clustering easy, well-understood, broad applicable, but unit value bias for heterogeneous strata
- Imputation and matching mostly give better results in a simulation study (especially matching)
- Drawbacks: arbitrary choices, unnatural to 'add' values to transaction data, interpretation difficulties.



Thank you!

